Register Allocation, ii

Graph coloring
Graph Coloring

**Idea:** reduce register allocation to graph coloring

- Create an interference graph for each program where:
  - nodes are variables
  - edges connect variables that cannot be in the same register
- Color the nodes in the graph such that connected nodes have different colors
- Each color represents a register; after coloring, read variable → register assignment from graph
Function with three variables, a, b, and c:

\[ f(x) = x^2 + x + 5 \]

```c
(:f
  1 0
  (a <- rdi)
  (b <- rdi)
  (b * b = b)
  (c <- 5)
  (rax <- b)
  (rax += c)
  (rax += a)
  (return))
```
Function with three variables, \(a\), \(b\), and \(c\):

\[ f(x) = x^2 + x + 5 \]

Black bars show the live ranges of the variables.
Three variables, and we needed three registers because we need three colors to color the graph
Different implementation of same function

(:f
    1 0
    (a <- rdi)
    (b <- rdi)
    (b * b)
    (c <- 5)
    (rax <- b)
    (rax + c)
    (rax + a)
    (return))

(:f
    1 0
    (a <- rdi)
    (b <- rdi)
    (b * b)
    (c <- 5)
    (rax <- b)
    (rax + c)
    (rax + a)
    (return))
Different implementation of same function

Less overlap in the live ranges of the variables; now we need fewer colors
Three variables, but we needed only two registers because we need only two colors to color the graph.

This makes sense because the live ranges of \( b \) and \( c \) didn’t overlap, so they can share a register.
NB: Those graphs are not accurate: they leave out the constraints imposed by the calling convention. We return to this later.
**Graph coloring algorithm:**

- Repeatedly select a node and remove it from the graph, putting it onto a stack

- When the graph is empty, rebuild it, putting a new color on each node as it comes back into the graph, making sure no adjacent nodes have the same color

- Order the colors; pick the smallest color that isn’t a neighbor, use that one

- If there are not enough colors, the algorithm fails (spilling comes in here)
With that ordering, we needed three colors, which is the best possible (because there was a connected subgraph of size 3)

But not all orderings work out so well
**Heuristic:** Remove the node with the most edges that’s smaller than the number of colors (registers) you want to use